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Conformational Characteristics of Poly(vinyl fluoride), Poly(fluoromethylene), and Poly(trifluoroethylene)

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ABSTRACT: Conformational energy estimates are employed to determine the conformational characteristics of poly(vinyl fluoride) (PVF), poly(fluoromethylene) (PFM), and poly(trifluoroethylene) (PTF₃). Effects of stereoconfiguration and, in the case of PVF and PTF₃, the presence of head-to-head:tail-to-tail (H-H:T-T) defect structures are considered. Rotational isomeric state models are developed for these polymers and used to calculate their unperturbed dimensions, dipole moments, and conformational entropies. The calculated results are compared to corresponding values found for poly(vinylidene fluoride), poly(tetrafluoroethylene), and polyethylene, and the equilibrium flexibilities of PVF, PFM, and PTF₃ are discussed on this basis.

During the course of our studies concerning the ¹³C NMR chemical shifts of vinyl polymers we became interested in understanding the ¹³C chemical shifts observed in the fluorinated polymers poly(tetrafluoroethylene) (PTFE), poly(vinylidene fluoride) (PVF₂), poly(vinyl fluoride) (PVF), poly(fluoromethylene) (PFM), and poly(trifluoroethylene) (PTF₃). We have demonstrated in hydrocarbon polymers, such as poly(propylene),^{1,2} ethylene-propylene copolymers,^{3,4} polystyrene,⁵ etc., and in a chlorine-substituted vinyl polymer [poly(vinyl chloride)⁶], that the chemical shift of a given carbon atom depends on the frequency with which it is involved in three bond gauche or γ interactions⁷⁻¹¹ with other carbon or chlorine atoms.

Each γ interaction produces an upfield chemical shift on the order of 3-5 ppm. Enumeration of the number and kind of γ interactions involving a given carbon atom permits¹¹ a determination of its relative ¹³C chemical shift. Bond rotation probabilities obtained from the rotational isomeric state (RIS) model^{12,13} of a polymer chain lead to just such an accounting of possible γ interactions.

With knowledge of the conformational characteristics of these polymers it was possible to understand their stereosequence-dependent ¹³C chemical shifts. Before the

same approach can be attempted for fluorinated polymers, we must possess information concerning their conformational characteristics.

The conformational characteristics of PTFE¹⁴ and PVF₂¹⁵ have been determined through approximate potential energy estimates¹⁶ and checked against experimentally determined unperturbed dimensions^{17,18} and dipole moments.¹⁴ However, neither PVF nor PFM nor PTF₃ have been studied from a conformational point of view. Such a study is described in this report, where the conformational energies of PVF, PFM, and PTF₃ chain fragments of various stereosequence are calculated, and where the possibility of head-to-head:tail-to-tail (H-H:T-T) addition of monomer units in PVF and PTF₃ is permitted and considered. From the conformational energies, RIS models are developed, and the conformationally sensitive properties $\langle r^2 \rangle_0$ and $\langle \mu^2 \rangle_0$, i.e., the mean-square unperturbed dimensions and dipole moments, and the conformational entropies, S_c , are calculated.

Conformational Energy Calculations

Portions of PVF (PTF₃) and PFM chains whose conformations depend on one or both of two neighboring bond rotation angles are illustrated in Figure 1. For PVF

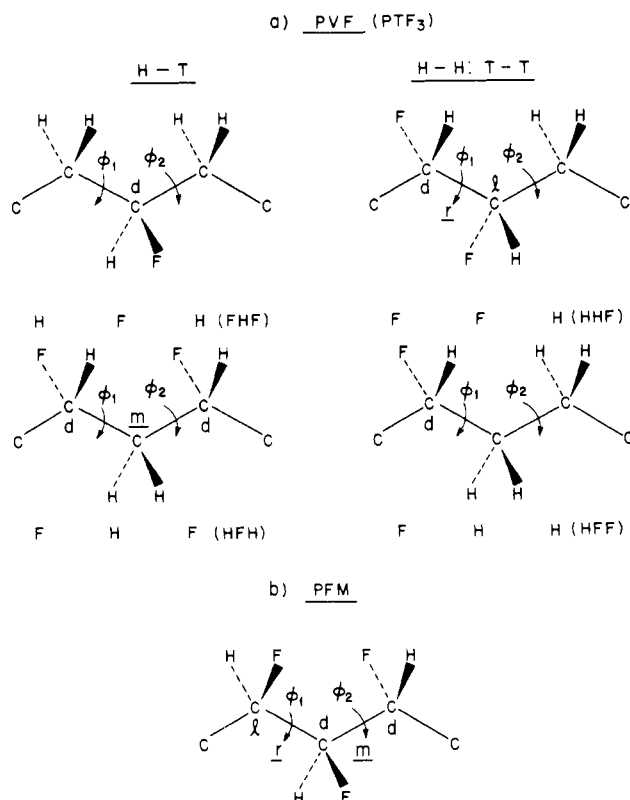


Figure 1. (a) PVF (PTF₃) chain fragments. CH₂ are replaced by CF₂ for PTF₃. (b) PFM chain fragments.

(PTF₃) both head-to-tail (H-T) HFH, FHF (FHF, HFH) and H-H:T-T FFH \leftrightarrow HFF, HHF \leftrightarrow FHH (HHF \leftrightarrow FHH, FFH \leftrightarrow HFF) chain fragments were considered. Conformational energies were calculated for each of these fragments as a function of the rotation angles ϕ_1 and ϕ_2 , using the approximate potential energy functions^{16,19} previously employed^{14,15} in the analysis of the conformational characteristics of PVF₂ and PTFE.

An intrinsic threefold torsional potential with a barrier height of 3.0 kcal/mol is assumed to separate three rotational minima at ϕ_1 or $\phi_2 = 0$ (trans, *t*), $\pm 120^\circ$ (gauche \pm , *g* \pm). A 6-12 potential describes nonbonded van der Waals interactions, and partial charges¹⁵ of ± 0.2 esu are assigned to the C and F atoms, respectively, terminating C-F bonds to account for nonbonded electrostatic interactions. A dielectric constant $\epsilon = 6$ was selected¹⁵ to mediate the electrostatic interactions.

Bond lengths of 1.53, 1.36, and 1.10 Å were used for C-C, C-F, and C-H bonds, and the valence angles²⁰ $\angle\text{CCC} = 112^\circ$ (PVF), 116° (PTF₃), 117.5° (PFM), $\angle\text{HCF} = \angle\text{FCF} = 106^\circ$, and $\angle\text{HCH} = 109.5^\circ$ were employed. Both rotation angles were stepped in 20° increments over their entire ranges.

Evaluation of RIS Models

Statistical weights $\text{SW}_{\alpha\beta}$ were evaluated for each of the nine pair-wise dependent rotational states $\alpha\beta = tt$, tg^\pm , $g^\pm t$, $g^\pm g^\pm$, and $g^\pm g^\mp$ from the calculated conformational energies. As an example,

$$\text{SW}_{g^+t} = \frac{\sum_{\phi_1=60^\circ}^{180^\circ} \sum_{\phi_2=-60^\circ}^{60^\circ} \exp[-E(\phi_1, \phi_2)/RT]}{\sum_{\phi_1=0}^{340^\circ} \sum_{\phi_2=0}^{340^\circ} \exp[-E(\phi_1, \phi_2)/RT]}$$

where the sums in both numerator and denominator contain only terms whose energies $E(\phi_1, \phi_2)$ are within 5.0 kcal/mol of the lowest energy conformation (ϕ_1, ϕ_2) found.

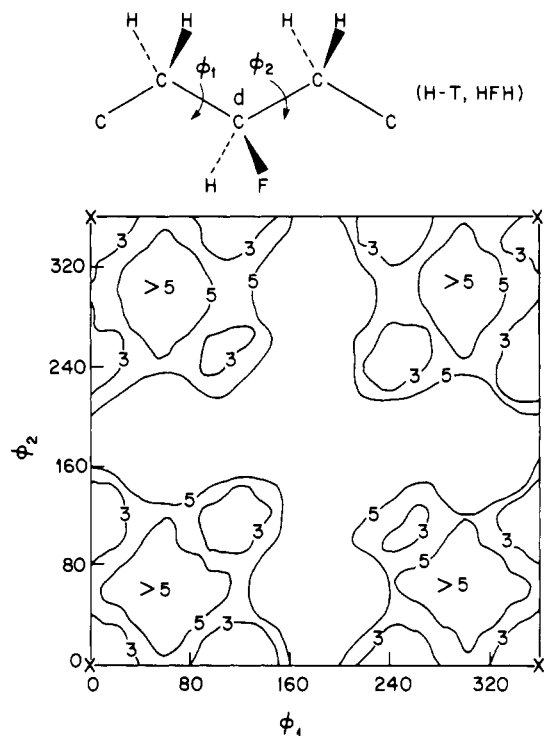


Figure 2. Conformational energy map for the HFH fragment in H-T PVF. Contours are in kcal/mol of fragment relative to the lowest energy conformation denoted by X.

Statistical weight matrices \mathbf{U} were then constructed at a given temperature. For PVF, as an example,

$$\mathbf{U}_{\text{HFH}} = \begin{matrix} \phi_1 \backslash \phi_2 & \begin{matrix} t & g^+ & g^- \end{matrix} \\ \begin{matrix} t \\ g^+ \\ g^- \end{matrix} & \begin{bmatrix} \text{SW}_{tt} & \text{SW}_{tg^+} & \text{SW}_{tg^-} \\ \text{SW}_{g^+t} & \text{SW}_{g^+g^+} & \text{SW}_{g^+g^-} \\ \text{SW}_{g^-t} & \text{SW}_{g^-g^+} & \text{SW}_{g^-g^-} \end{bmatrix} \end{matrix}$$

One such statistical weight matrix was constructed for each different chain fragment (see Figure 1) considered in PVF, PFM, and PTF₃ at $T = 0, 50, 100, 150$, and 200°C . These matrices define the RIS model appropriate to each polymer.

Calculation of Dimensions, Dipole Moments, and Conformational Entropies

Matrix multiplication techniques¹³ were used to calculate mean-square end-to-end distances $\langle r^2 \rangle_0$, dipole moments $\langle \mu^2 \rangle_0$, and conformational entropies S_c of isolated and unperturbed PVF, PFM, and PTF₃ chains. A C-F bond dipole moment²¹ of 1.8 D was used in the calculation of $\langle \mu^2 \rangle_0$. Chains of 400–500 backbone bonds were considered. Each chain was generated a bond at a time by Monte-Carlo techniques and checked for the effects of stereosequence and (H-H:T-T) defect content at each bond addition. Ten Monte-Carlo chains were generated for each defect content and each degree of stereoregularity, and $\langle r^2 \rangle_0$, $\langle \mu^2 \rangle_0$, and S_c were averaged over the same ensemble of chains.

Calculated Results

Figures 2–6 present conformational energy maps for representative fragments of the PVF and PFM chains. Statistical weight matrices for all possible PVF, PFM, and PTF₃ chain fragments are given in the Appendix at $T = 0, 50, 100, 150, 200^\circ\text{C}$. The dimensions and dipole moments presented as the ratios $\langle r^2 \rangle_0/nl^2$ and $\langle \mu^2 \rangle_0/nm^2$, where n is the number of bonds in the chain, l^2 is the square of the C-C bond length, and m^2 is the square of the C-F bond dipole moment ($1/2$ and $3/2$ the square for PVF and PTF₃), appear in Tables I and II. Temperature

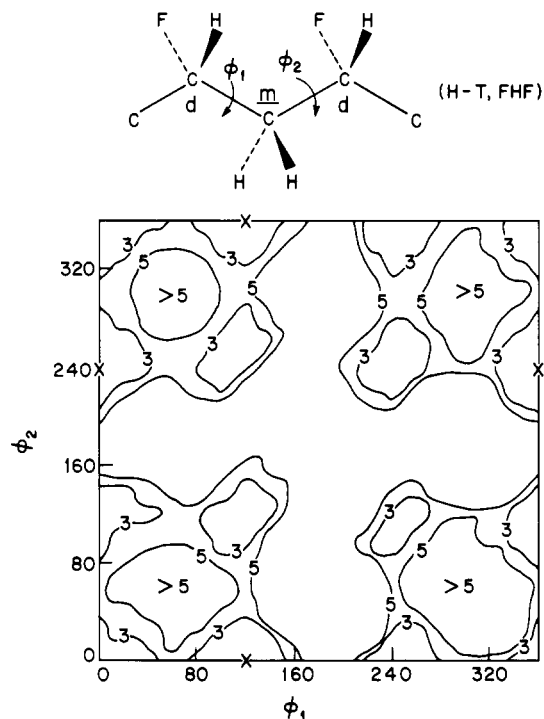


Figure 3. Same as Figure 2 except replace HFH with FHF.

TABLE I

$$\frac{\langle r^2 \rangle_0}{nl^2}$$

and

$$\frac{\langle \mu^2 \rangle_0}{nm^2}$$

calculated for 400-500 Bond PVF and PTF₃
Chains as a Function of
Stereoregularity and H-H:T-T
Defect Content.

%H-H:T-T	P _m ^a	PVF				PTF ₃			
		$\langle r^2 \rangle_0/nl^2$		$\langle \mu^2 \rangle_0/nm^2$		$\langle r^2 \rangle_0/nl^2$		$\langle \mu^2 \rangle_0/nm^2$	
0	0	7.2 ^b	6.1 ^c	1.28 ^b	1.15 ^c	9.9 ^b	8.9 ^c	0.54 ^b	0.52 ^c
"	.2	7.7	6.4	1.23	1.12	10.3	9.0	0.56	0.52
"	.4	8.0	6.5	1.20	1.10	10.5	9.0	0.57	0.52
"	.6	8.1	6.5	1.20	1.09	10.5	9.0	0.57	0.52
"	.8	7.8	6.3	1.22	1.12	10.3	9.0	0.56	0.52
"	1.0	7.2	6.1	1.28	1.16	9.9	8.9	0.54	0.52
10	0	7.2	6.0	1.06	1.00	10.8	9.5	0.43	0.43
"	.2	7.4	6.1	1.13	1.06	10.5	9.3	0.48	0.46
"	.4	7.7	6.3	1.08	1.01	10.9	9.4	0.48	0.45
"	.6	7.8	6.3	1.04	1.00	11.1	9.4	0.47	0.43
"	.8	7.6	6.3	1.05	0.99	11.0	9.5	0.47	0.44
"	1.0	7.2	6.0	1.08	1.02	10.7	9.4	0.44	0.44
20	0	7.1	6.0	0.90	0.90	11.6	9.9	0.35	0.37
"	.2	7.0	5.8	1.08	1.02	10.6	9.5	0.43	0.42
"	.4	7.3	6.0	1.00	0.95	11.1	9.7	0.42	0.40
"	.6	7.6	6.2	0.93	0.92	11.6	9.7	0.40	0.38
"	.8	7.5	6.1	0.91	0.89	11.8	9.9	0.38	0.38
"	1.0	7.2	6.0	0.93	0.92	11.5	9.9	0.37	0.36
30	0	7.1	5.9	0.79	0.80	12.4	10.4	0.30	0.32
"	.2	7.0	5.8	0.94	0.91	11.3	9.9	0.36	0.36
"	.4	7.1	5.9	0.94	0.93	11.3	9.8	0.37	0.37
"	.6	7.4	6.0	0.87	0.85	11.9	10.1	0.36	0.35
"	.8	7.4	6.0	0.80	0.82	12.4	10.3	0.33	0.32
"	1.0	7.1	5.9	0.79	0.82	12.3	10.2	0.30	0.32

a - Probability of a meso (*m*) dyad (see Figure 1(a))

b - T = 50°C

c - T = 150°C

coefficients of $\langle r^2 \rangle_0$ and $\langle \mu^2 \rangle_0$ are presented in Tables III and IV.

Discussion and Results

Both the calculated dimensions and dipole moments of PVF are virtually independent of stereosequence. Fur-

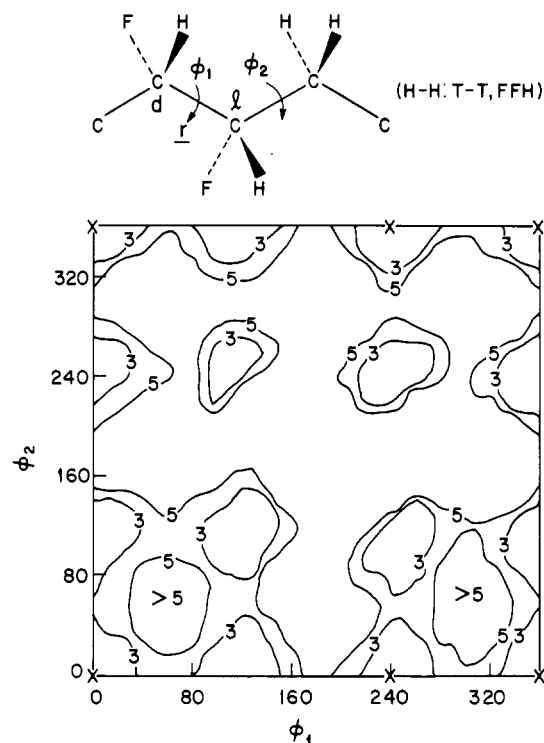


Figure 4. Same as Figure 2 except replace HFH with FFH and H-T with H-H:T-T.

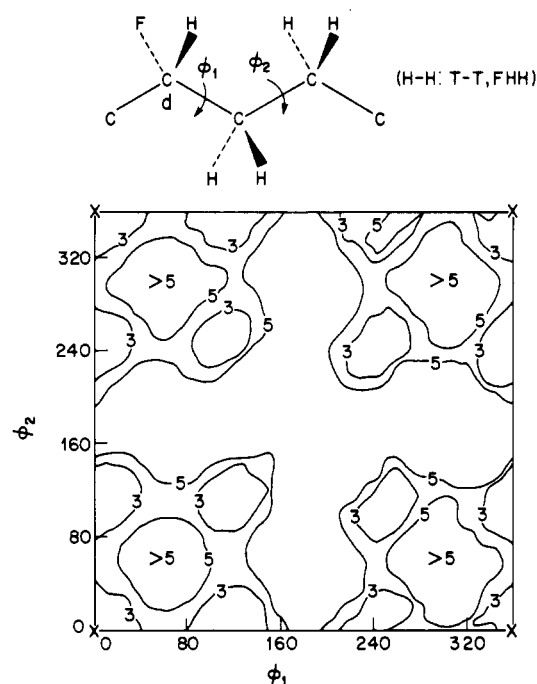


Figure 5. Same as Figure 4 except replace FFH with FHH.

Table II
 $\langle r^2 \rangle_0/nl^2$ and $\langle \mu^2 \rangle_0/nm^2$
Calculated for 400 Bond PFM Chains as a
Function of Stereoregularity

P _m ^a	$\langle r^2 \rangle_0/nl^2$		$\langle \mu^2 \rangle_0/nm$	
	50 °C	150 °C	50 °C	150 °C
0	13.3	10.4	2.11	1.67
0.2	10.5	8.54	1.58	1.39
0.4	8.57	7.30	1.17	1.07
0.6	7.07	6.06	0.86	0.83
0.8	5.81	5.13	0.58	0.60
1.0	5.01	4.95	0.36	0.40

^a Probability of a meso (*m*) dyad (see Figure 1b).

TABLE III

$d \ln \langle r^2 \rangle_0 / dT$
and $d \ln \langle \mu^2 \rangle_0 / dT$
for PVF and PTF₃ Chains of 400-500 Bonds
of Varying Stereoregularities and
H-H:T-T Defect Contents

%H-T:T-T	P _m ^a	$(d \ln \langle r^2 \rangle_0 / dT)^b, K^{-1}$		$(d \ln \langle \mu^2 \rangle_0 / dT)^b, K^{-1}$	
		PVF	PTF ₃	PVF	PTF ₃
0	0	-0.0017	-0.0011	-0.0010	-0.0004
"	.2	-0.0018	-0.0013	-0.0009	-0.0007
"	.4	-0.0021	-0.0015	-0.0009	-0.0009
"	.6	-0.0022	-0.0015	-0.0010	-0.0009
"	.8	-0.0021	-0.0013	-0.0009	-0.0007
"	1.0	-0.0017	-0.0011	-0.0010	-0.0004
10	0	-0.0018	-0.0013	-0.0006	0.0
"	.2	-0.0019	-0.0012	-0.0006	-0.0004
"	.4	-0.0020	-0.0015	-0.0007	-0.0006
"	.6	-0.0021	-0.0017	-0.0004	-0.0009
"	.8	-0.0019	-0.0015	-0.0006	-0.0007
"	1.0	-0.0018	-0.0013	-0.0006	0.0
20	0	-0.0017	-0.0016	0.0	+0.0006
"	.2	-0.0019	-0.0011	-0.0006	-0.0002
"	.4	-0.0020	-0.0013	-0.0005	-0.0005
"	.6	-0.0020	-0.0018	-0.0001	-0.0005
"	.8	-0.0021	-0.0018	-0.0002	0.0
"	1.0	-0.0018	-0.0015	-0.0001	-0.0003
30	0	-0.0018	-0.0018	+0.0001	+0.0006
"	.2	-0.0019	-0.0013	-0.0003	0.0
"	.4	-0.0018	-0.0014	-0.0001	0.0
"	.6	-0.0021	-0.0016	-0.0002	-0.0003
"	.8	-0.0021	-0.0019	+0.0002	-0.0003
"	1.0	-0.0018	-0.0019	+0.0004	+0.0006

a - Probability of meso (*m*) dyad (see Figure 1(a))b - $dT = 150-50 = 100^\circ C$

TABLE IV
 $d \ln \langle r^2 \rangle_0 / dT$ and $d \ln \langle \mu^2 \rangle_0 / dT$
for 400 Bond PFM Chains of Differing Stereoregularity

P_n^a	$d \ln \langle r^2 \rangle_0 / dT, K^{-1}$	$d \ln \langle \mu^2 \rangle_0 / dT, K^{-1}$
0	-0.0024	-0.0023
0.2	-0.0021	-0.0013
0.4	-0.0018	-0.0009
0.6	-0.0015	-0.0004
0.8	-0.0012	+0.0003
1.0	-0.0012	+0.0011

^a Probability of meso (*m*) dyad (see Figure 1b). ^b $dT = 150 - 50 = 100^\circ C$.

thermore the dimensions are also insensitive to the level of H-H:T-T addition. The characteristic ratios $CR = \langle r^2 \rangle_0 / nl^2$ calculated for PVF do not vary more than 10-15% over the entire spectrum of stereoregularity even allowing for as many as 30% H-H:T-T additions. Dipole moment ratios $CM = \langle \mu^2 \rangle_0 / nm^2$, although independent of stereosequence, do decrease 20-25% as the H-H:T-T content reaches 20-30%.

Neither property can be usefully employed to determine PVF stereoregularity, and they both fail to exhibit any marked degree of sensitivity to H-H:T-T defect content. These two conformational properties cannot be expected to characterize the microstructure of PVF.

Table V
Comparison of Unperturbed Dimensions

polymer	CR ^a	$d \ln \langle r^2 \rangle_0 / dT^b$
PE ^c	6.7	-0.0011
PVF	6.0	-0.0020
PVF ₂ ^c	5.9	-0.0013
PFM	4.5-10.5 ^d	-0.0012-0.0024 ^d
PTF ₃	9.5	-0.0020
PTFE ^c	30	-0.0009

^a $T = 150^\circ C$. ^b Calculated for $dT = 150 - 50 = 100^\circ C$.
^c Experimentally confirmed.^{13,14,17,18} ^d Range corresponds to $P_m = 1.0-0.0$.

Table VI
Conformational Entropies Calculated at $150^\circ C$

polymer	S_c , eu/(mol bonds)
PE	1.8
PVF	(2.1-2.3) ^a
PVF ₂	2.0
PFM	(1.9-2.6) ^b
PTF ₃	(1.8-2.0) ^c
PTFE	1.4

^a Corresponds to $P_m = 0.0-1.0$ and 0% H-H:T-T addition. ^b Corresponds to $P_m = 1.0-0.0$. ^c Corresponds to $P_m = 1.0-0.0$ and 0% H-H:T-T addition.

Both CR and CM are sensitive to chain stereoregularity in PFM. As the probability of meso (*m*) dyad placement decreases from 1.0 to 0.0, CR and CM increase 2-3- and 4-6-fold, respectively. Clearly, either property can be expected to successfully characterize the stereoregularity of PFM chains.

Neither CR nor CM are sensitive to chain stereoregularity in PTF₃. As for PVF chains, only CM is significantly affected by H-H:T-T addition and may possibly be used to characterize the defect content of PTF₃ chains.

Inspection of the statistical weight matrices of PVF (see Appendix) indicates that several conformations, or (ϕ_1, ϕ_2) pairs of bond rotations, are likely regardless of stereosequence or defect content. Also note the similarities among the conformational energy maps of PVF fragments (Figures 2-5) corresponding to both H-T and H-H:T-T addition of monomer units. The similar degree of conformational diversity among all possible PVF chain fragments produces the nearly constant dimensions calculated for PVF chains of any likely structure. These comments are also applicable to PTF₃, with the additional observation that the larger dimensions [$CR = 9.5$ (PTF₃), 6.0 (PVF)] result from a significant increase in the probability of the all-trans (*t*), planar zigzag conformation.

The PFM chain, on the other hand, increasingly prefers the extended *tt* conformation as the meso (*m*) placement of dyads decreases. (The all-meso chain prefers the $tg^\pm, g^\pm t$ conformations, which result in compact chain conformations.) Hence, the all-racemic (*r*) chain has dimensions 2-3 times as large as all-meso (*m*) PFM.

PVF, PFM, and PTF₃ are all expected to contract with increasing temperature as indicated by the temperature coefficients of the dimensions, $d \ln \langle r^2 \rangle_0 / dT$, presented in Tables III and IV. Stereosequence and defect content have little effect on the ability of these polymer chains to adopt more compact conformations as the temperature is raised.

It may be of interest to compare the conformational characteristics of PVF, PFM and PTF₃ with those of PVF₂, PTFE, and polyethylene (PE) to learn how the increasing

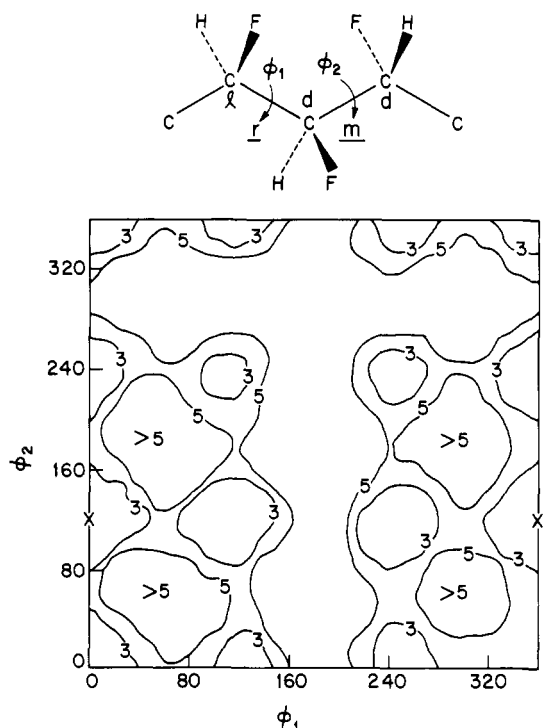


Figure 6. Conformational energy map for the r, m chain fragment of PFM. Contours are in kcal/mol of fragment relative to the lowest energy conformation denoted by \times .

fluorination of PE affects equilibrium chain extension. In Table V the calculated dimensions (CR) and their temperature coefficients are presented for PE, PVF, PFM, PVF₂, PTF₃, and PTFE. With the exceptions of the completely fluorinated member (PTFE) and predominantly isotactic PFM chains (with PM = 0.0–0.2), all members of this polymer series have dimensions which are remarkably similar, i.e., CR = 5–9. In addition, each polymer chain contracts with increasing temperature to adopt more compact conformations. This chain contraction is characterized by $d \ln \langle r^2 \rangle_0 / dT = -(0.001-0.002) \text{ K}^{-1}$ for each of these polymers.

Although the conformational characteristics of PVF, PFM, and PTF₃ chains remain to be tested experimentally, it would appear that except for PTFE all of the polymers in this series possess comparable equilibrium extensions as manifested by their unperturbed dimensions. In addition, Table VI presents conformational entropies, S_c , calculated^{22,23} at 150 °C for each polymer. Conformational entropy provides a measure of the number and frequency of occurrence of the various bond rotational states. Thus, CR and S_c , which are two distinctly different²⁴ probes of polymer chain conformations, both indicate that this series of polymers, with the exception of PTFE, possesses similar conformational characteristics.²⁵

Acknowledgment. Happy Birthday Professor Flory.

Appendix: Statistical Weight Matrices⁺ for PVF, PFM, and PTF₃ Chains at 0, 50, 100, 150, and 200 °C

PVF(H-T)					PTF ₃ (H-T)				
FHF(dd) =	$\phi_1 \backslash \phi_2$	t	g^+	g^-	HFH(dd) =	$\phi_1 \backslash \phi_2$	t	g^+	g^-
		.153 ^a	.114	.202			.358 ^a	.261	.051
	t	.151 ^b	.115	.188		.333 ^b	.253	.064	
		.149 ^c	.115	.179		.313 ^c	.244	.075	
		.148 ^d	.114	.172		.297 ^d	.235	.084	
		.147 ^e	.113	.167		.284 ^e	.227	.091	
		g^+	.202	.068		.067	.051	.009	0.0
	.188		.074	.077		.064	.015	0.0	
	.179		.078	.082		.075	.021	.001	
	.172		.082	.086		.084	.027	.001	
	.167		.085	.089		.091	.032	.002	
	g^-	.116	.011	.067		.261	.001	.009	
		.118	.016	.073		.253	.003	.015	
		.119	.021	.078		.245	.005	.021	
		.119	.026	.081		.236	.008	.027	
.119		.030	.083	.229	.010	.032			

- a – T = 0°C
 b – T = 50°C
 c – T = 100°C
 d – T = 150°C
 e – T = 200°C

PVF(H-T)

$\phi_1 \backslash \phi_2$				$\phi_1 \backslash \phi_2$			
	t	g^+	g^-		t	g^+	g^-
FHF(dl) =	.347	.118	.092	HFH(d) =	.314	.147	.163
	.301	.122	.096		.276	.148	.165
	t	.271	.125		t	.251	.147
		.249	.126			.235	.145
		.233	.127			.223	.143
		.120	.112			.160	.047
	g^+	.125	.114		g^+	.162	.055
		.127	.115			.161	.062
		.128	.115			.159	.067
		.129	.115			.156	.071
		.099	.037			.114	.005
	g^-	.105	.046		g^-	.122	.008
		.108	.052			.126	.012
		.110	.058			.129	.016
		.112	.062			.130	.020
		.032	.038			.041	.050
		.043	.047			.057	.062
		.051	.051			.067	.067

PTF₃(H-T)

$\phi_1 \backslash \phi_2$				$\phi_1 \backslash \phi_2$			
	t	g^+	g^-		t	g^+	g^-
FHF(dl) =	.629	.082	.065	FHF(d) =	.151	.151	.219
	.539	.099	.082		.151	.147	.205
	t	.472	.112		t	.149	.144
		.423	.120			.149	.140
		.386	.126			.148	.137
		.082	.001			.215	.066
	g^+	.099	.002		g^+	.201	.076
		.112	.004			.192	.084
		.120	.006			.184	.089
		.126	.008			.178	.092
		.065	.001			.075	.003
	g^-	.082	.001		g^-	.083	.005
		.095	.003			.088	.008
		.103	.004			.093	.011
		.110	.006			.096	.014
		.074	.074			.099	.099
		.094	.107			.102	.104
		.116	.122			.104	.105

Interchanging the second and third columns and rows of FHF(dd), FHF(dl), and HFH(d) yields FHF(ll), FHF(ld), and HFH(l), respectively. Interchange H and F for PTF₃.

PVF (H-H:T-T)

$\phi_1 \backslash \phi_2$				$\phi_1 \backslash \phi_2$			
	t	g^+	g^-		t	g^+	g^-
FFH(dl) =	.195	.114	.098	FFH(dd) =	.268	.067	.239
	.184	.118	.100		.245	.074	.217
	t	.176	.120		t	.228	.079
		.171	.122			.215	.083
		.167	.123			.206	.086
		.146	.126		g^+	.111	.060
	g^+	.144	.125			.115	.065
		.142	.124			.118	.069
		.140	.123			.120	.072
		.139	.122			.121	.074
	g^-	.199	.053		g^-	.145	.013
		.188	.061			.152	.019
		.181	.067			.154	.024
		.175	.071			.155	.028
		.170	.074			.155	.032
		.052	.057			.058	.065
		.060	.063			.070	.074
		.066	.066			.077	.077

PTF₃(H-H:T-T)

$\phi_1 \backslash \phi_2$		t	g^+	g^-
HHF(dl) =	t	.255	.288	.018
		.246	.274	.027
		.238	.261	.035
		.230	.249	.042
		.224	.239	.049
	g^+	.094	.009	0.0
		.107	.015	0.0
		.116	.021	.001
		.122	.027	.001
		.127	.033	.002
	g^-	.294	.003	.039
		.275	.007	.050
		.259	.011	.060
		.246	.015	.067
		.235	.020	.073

$\phi_1 \backslash \phi_2$		t	g^+	g^-
HHF(dd) =	t	.399	.107	.119
		.357	.117	.126
		.326	.124	.131
		.302	.128	.134
		.284	.131	.136
	g^+	.230	.005	.002
		.225	.010	.004
		.219	.015	.006
		.213	.020	.009
		.207	.024	.012
	g^-	.086	0.0	.052
		.097	0.0	.065
		.105	.001	.074
		.110	.002	.082
		.114	.002	.088

Interchanging the second and third columns and rows of FFH(dl) and FFH(dd) yields FFH(ld) and FFH(ll). Each of the HFF matrices can be obtained from the appropriate FFH matrix via total interchange of elements. As an example, $FHH(dd)[I,J] = FFH(dd)[J,I]$. Interchange H and F for PTF₃.

PVF (H-H:T-T)

$\phi_1 \backslash \phi_2$		t	g^+	g^-
FHH(d) =	t	.270	.116	.140
		.245	.118	.143
		.226	.119	.143
		.213	.119	.142
		.203	.120	.140
	g^+	.143	.074	.025
		.140	.081	.033
		.138	.086	.041
		.136	.090	.047
		.135	.092	.052
	g^-	.122	.025	.085
		.117	.033	.090
		.114	.040	.093
		.113	.046	.094
		.112	.051	.095

PTF₃ (H-T:T-T)

		t	g^+	g^-
t	HFF(d) =	.432	.157	.067
		.382	.164	.080
		.345	.166	.089
		.317	.167	.096
		.295	.166	.102
g^+		.122	.009	.001
		.132	.014	.003
		.137	.020	.005
		.141	.026	.007
		.143	.031	.009
g^-		.172	.003	.037
		.175	.005	.046
		.176	.008	.054
		.174	.012	.061
		.173	.015	.067

FHH(l) is obtained from FHH(d) by interchanging second and third columns and rows, and HFF(d) and HFF(l) are obtained by a total interchange ($I,J \rightarrow J,I$) of the elements of FHH(d) and FHH(l). Interchange H and F for PTF₃.

PFM

$\phi_1 \backslash \phi_2$	t	g^+	g^-
t	.036	.028	.257
	.045	.037	.237
	.053	.045	.221
	.059	.052	.208
	.065	.058	.198
III =	.314	.074	.161
	.283	.083	.165
	.259	.090	.166
	.241	.095	.166
	.227	.098	.165
g^+	.042	.003	.085
	.052	.005	.097
	.060	.008	.098
	.066	.011	.102
	.071	.014	.104

$\phi_1 \backslash \phi_2$	t	g^+	g^-
t	.218	.312	.084
	.207	.283	.093
	.198	.262	.098
	.191	.245	.102
	.184	.233	.105
ldd =	.024	.183	.006
	.032	.177	.011
	.040	.172	.015
	.046	.166	.020
	.051	.161	.025
g^+	.093	.069	.011
	.100	.080	.017
	.105	.088	.022
	.108	.094	.028
	.110	.098	.033

$\phi_1 \backslash \phi_2$	t	g^+	g^-
t	.321	.129	.119
	.291	.134	.123
	.268	.137	.125
	.251	.138	.125
	.238	.139	.125
ldl =	.178	.030	.006
	.174	.039	.009
	.169	.047	.013
	.165	.054	.017
	.161	.060	.021
g^+	.173	.014	.030
	.170	.021	.039
	.167	.028	.046
	.164	.034	.052
	.161	.039	.056

$\phi_1 \backslash \phi_2$	t	g^+	g^-
t	.214	.016	.060
	.205	.023	.071
	.197	.029	.079
	.190	.035	.085
	.184	.039	.090
ldd =	.355	.156	.061
	.319	.154	.073
	.293	.150	.083
	.274	.146	.090
	.258	.142	.095
g^+	.120	.006	.012
	.126	.010	.019
	.129	.015	.025
	.131	.019	.030
	.132	.024	.036

Interchanging second and third columns and rows of lll, ldl, ldd, and lld yields ddd, dld, dll, and ddl, respectively.

+ In the calculation of conformational entropies, S_c , all elements of each statistical weight matrix must be divided by the largest element corresponding to a given temperature. As an example, the elements of $FHF(dd)$ (PVF) must be divided by .153, .151, .149, .148, and .147 when calculating S_c at $T = 0, 50, 100, 150$ and 200°C , respectively.

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